

29.43. Model: Mechanical energy is conserved.

Visualize: Please refer to Figure P29.43. Label the 5.0 nC charge with subscript 1, the 3.0 nC with subscript 2, and so on.

Solve: The conservation of energy equation $K_f + U_f = K_i + U_i$ is

$$K_f + 0 \text{ J} = 0 \text{ J} + U_i \Rightarrow K_f = U_i = U_{12} + U_{13} + U_{14} + U_{23} + U_{24} + U_{34}$$

$$U_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_{12}} = \frac{(9.0 \times 10^9 \text{ N m}^2 / \text{C}^2)(5.0 \times 10^{-9} \text{ C})(3.0 \times 10^{-9} \text{ C})}{0.035 \text{ m}} = 3.857 \times 10^{-6} \text{ J}$$

$$U_{13} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_3}{r_{13}} = \frac{(9.0 \times 10^9 \text{ N m}^2 / \text{C}^2)(5.0 \times 10^{-9} \text{ C})(4.0 \times 10^{-9} \text{ C})}{\sqrt{(0.035 \text{ m})^2 + (0.015 \text{ m})^2}} = 4.727 \times 10^{-6} \text{ J}$$

$$U_{14} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_4}{r_{14}} = \frac{(9.0 \times 10^9 \text{ N m}^2 / \text{C}^2)(5.0 \times 10^{-9} \text{ C})(2.0 \times 10^{-9} \text{ C})}{0.015 \text{ m}} = 6.000 \times 10^{-6} \text{ J}$$

Likewise, $U_{23} = 7.200 \times 10^{-6} \text{ J}$, $U_{24} = 1.418 \times 10^{-6} \text{ J}$, and $U_{34} = 2.057 \times 10^{-6} \text{ J}$. The sum of all the potential energies is $25.3 \times 10^{-6} \text{ J}$, which is the final kinetic energy K_f .